The midterm grades were released and we accept regrades until next Tuesday (EOD)

- COS484
  - max: 50, median: 39.75, std: 5.95

- COS584
  - max: 49, median: 37, std: 5.76
Announcements

• The project guideline (484 and 584 separately) has been released!
• The proposal deadline is changed to next Friday (March 26)
  • 1 page, not graded
• 484: 3 students per team
  • Two options: (a) reproducing a recent NLP paper (encouraged) (2) research project
• 584: 1-2 students per team, research project
• If you can’t find a partner yet, use the thread in Ed and we will try to help you.
Announcements

- Assignment 2 due today
- Assignment 3 out today and due on **March 31**
- COS484 precept this Friday
  - Our TAs will give a tutorial on PyTorch.
  - If you don’t have enough experience with PyTorch before, you are highly encouraged to attend the 484 precept—the programming problems of assignment 3 & 4 require the use of PyTorch.
Recap: Recurrent Neural Networks

$h_0 \in \mathbb{R}^h$ is an initial state

$h_t = f(h_{t-1}, x_t) \in \mathbb{R}^h$

$h_t$: hidden states which store information from $x_1$ to $x_t$

**Simple RNNs:**

$$h_t = g(W h_{t-1} + U x_t + b) \in \mathbb{R}^h$$

$g$: nonlinearity (e.g. tanh),

$W \in \mathbb{R}^{h \times h}$, $U \in \mathbb{R}^{h \times d}$, $b \in \mathbb{R}^h$

**RNNLMs:**
This lecture

- More applications: sequence tagging, text classification
- More variants: multi-layer RNNs, bidirectional RNNs
- More advanced types of RNNs: LSTMs, GRUs
Application: Sequence Tagging

Input: a sentence of $n$ words: $x_1, \ldots, x_n$
Output: $y_1, \ldots, y_n$, $y_i \in \{1, \ldots, C\}$

$$P(y_i = k) = \text{softmax}_k(W_o h_i) \quad W_o \in \mathbb{R}^{C \times h} \quad L = -\frac{1}{n} \sum_{i=1}^{n} \log P(y_i = k)$$

A better solution is to use RNNs + conditional random field (CRF), see Lample et al., 2016 for more details
Application: Text Classification

Input: a sentence of \( n \) words

Output: \( y \in \{1, 2, \ldots, C\} \)

\[
P(y = k) = \text{softmax}_k(W_o h_n) \quad W_o \in \mathbb{R}^{C \times h}
\]

\[
L = -\log P(y = c)
\]
Multi-layer RNNs

- RNNs are already “deep” on one dimension (unroll over time steps)
- We can also make them “deep” in another dimension by applying multiple RNNs
- Multi-layer RNNs are also called **stacked RNNs**.
Multi-layer RNNs

The hidden states from RNN layer $i$ are the inputs to RNN layer $i + 1$

- In practice, using 2 to 4 layers is common (usually better than 1 layer)
- Transformer networks can be up to 24 layers with lots of skip-connection.
Bidirectional RNNs

\( h_t \) : hidden states which store information from \( x_1 \) to \( x_t \)

- Bidirectionality is important in language representations:

  - **Left context** “the movie was”
  - **Right context** “exciting!”

**terribly:**
- left context “the movie was”
- right context “exciting!”
Bidirectional RNNs

\[
\begin{align*}
\mathbf{h}_t &= f_1(\mathbf{h}_{t-1}, \mathbf{x}_t), t = 1, 2, \ldots n \\
\mathbf{\hat{h}}_t &= f_2(\mathbf{\hat{h}}_{t+1}, \mathbf{x}_t), t = n, n-1, \ldots 1 \\
\mathbf{h}_t &= [\mathbf{h}_t, \mathbf{\hat{h}}_t] \in \mathbb{R}^{2h}
\end{align*}
\]
Can we use bidirectional RNNs in the following tasks?

(1) text classification, (2) sequence tagging, (3) text generation

(a) Yes, Yes, Yes
(b) Yes, No, Yes
(c) Yes, Yes, No
(d) No, Yes, No

The answer is (c).
Bidirectional RNNs

- Sequence tagging: Yes! (esp. important)
Bidirectional RNNs

• Sequence tagging: Yes!

• Text classification: Yes!
  • Common practice: concatenate the last hidden vectors in two directions or take the mean/max over all the hidden vectors

• Text generation: No. Because we can’t see the future to predict the next word.

```
the movie was terribly exciting!
```
Bidirectional RNNs

- Bidirectional RNNs are only applicable if you have access to the entire input sequence.
- If you do have the entire input sequence, bidirectionality is powerful (and you should use it by default).
- Modeling the bidirectionality is the key idea behind BERT (BERT = Bidirectional Encoder Representations from Transformers).
  - We will learn Transformers and BERT in a few weeks!
- A very common choice for sentence/document modeling: multi-layer bidirectional RNNs.
Advanced RNN variants

LSTMs

\[
\begin{align*}
    i_t &= \sigma(W^i h_{t-1} + U^i x_t + b^i) \\
    f_t &= \sigma(W^f h_{t-1} + U^f x_t + b^f) \\
    o_t &= \sigma(W^o h_{t-1} + U^o x_t + b^o) \\
    g_t &= \tanh(W^g h_{t-1} + U^g x_t + b^g) \\
    c_t &= c_{t-1} \odot f_t + g_t \odot i_t \\
    h_t &= \tanh(c_t) \odot o_t
\end{align*}
\]

GRUs

\[
\begin{align*}
    r_t &= \sigma(W^r h_{t-1} + U^r x_t + b^r) \\
    z_t &= \sigma(W^z h_{t-1} + U^z x_t + b^z) \\
    \tilde{h}_t &= \tanh(W(r_t \odot h_{t-1}) + Ux_t + b) \\
    h_t &= (1 - z_t) \odot h_{t-1} + z_t \odot \tilde{h}_t
\end{align*}
\]

\[
\begin{align*}
    h_t &= f(h_{t-1}, x_t) \in \mathbb{R}^h \\
    h_t &= \tanh(Wh_{t-1} + Ux_t + b) \in \mathbb{R}^h
\end{align*}
\]
Long Short-Term Memory RNNs (LSTMs)

- A type of RNN proposed by Hochreiter and Schmidhuber in 1997 as a solution to the vanishing gradients problem.
  - Everyone cites that paper but really a crucial part of the modern LSTM is from Gers et al. (2000)

LONG SHORT-TERM MEMORY


Sepp Hochreiter
Fakultät für Informatik
Technische Universität München
80290 München, Germany
hochreit@informatik.tu-muenchen.de
http://www7.informatik.tu-muenchen.de/~hochreit

Jürgen Schmidhuber
IDSIA
Corso Elvezia 36
6900 Lugano, Switzerland
juergen@idsia.ch
http://www.idsia.ch/~juergen

Learning to Forget: Continual Prediction with LSTM

Felix A. Gers
Jürgen Schmidhuber
Fred Cummins
IDSIA, 6900 Lugano, Switzerland
Recap: Vanishing Gradient Problem

\[ h_2 = g(Wh_1 + Ux_2 + b) \]
\[ h_3 = g(Wh_2 + Ux_3 + b) \]
\[ L_3 = -\log \hat{y}_3(w_4) \]

\[ \frac{\partial L_3}{\partial W} = \frac{\partial L_3}{\partial h_3} \frac{\partial h_3}{\partial W} + \frac{\partial L_3}{\partial h_3} \frac{\partial h_3}{\partial h_2} \frac{\partial h_2}{\partial W} + \frac{\partial L_3}{\partial h_3} \frac{\partial h_3}{\partial h_2} \frac{\partial h_2}{\partial h_1} \frac{\partial h_1}{\partial W} \]

\[ \frac{\partial L}{\partial W} = -\frac{1}{n} \sum_{t=1}^{n} \sum_{k=1}^{t} \frac{\partial L_t}{\partial h_t} \left( \prod_{j=k+1}^{t} \frac{\partial h_j}{\partial h_{j-1}} \right) \frac{\partial h_k}{\partial W} \]

If \( k \) and \( t \) are far away, the gradients are very easy to grow/shrink exponentially (called the gradient exploding or gradient vanishing problem)
Recap: Vanishing Gradient Problem

When she tried to print her tickets, she found that the printer was out of toner. She went to the stationery store to buy more toner. It was very overpriced. After installing the toner into the printer, she finally printed her ________
**LSTMs: The intuition**

- Key idea: turning **multiplication** into **addition** and using “**gates**” to control how much information to add/erase.

- At each time step, instead of re-writing the hidden state $h_t = g(Wh_{t-1} + Ux_t + b)$, there is also a cell state $c_t \in \mathbb{R}^h$ which stores **long-term information**.

  - We write to/erase information from $c_t$ after each step.

  - We read $h_t$ from $c_t$.

- Diagram illustrating the flow of information through $c_t$ and $h_t$.
LSTMs: the formulation

- **Input gate** *(how much to write)*:
  
  \[ i_t = \sigma(W_i h_{t-1} + U_i x_t + b_i) \in \mathbb{R}^h \]

- **Forget gate** *(how much to erase)*:
  
  \[ f_t = \sigma(W_f h_{t-1} + U_f x_t + b_f) \in \mathbb{R}^h \]

- **Output gate** *(how much to reveal)*:
  
  \[ o_t = \sigma(W_o h_{t-1} + U_o x_t + b_o) \in \mathbb{R}^h \]

- **New memory cell** *(what to write)*:
  
  \[ g_t = \tanh(W_g h_{t-1} + U_g x_t + b_g) \in \mathbb{R}^h \]

- **Final memory cell**:
  
  \[ c_t = f_t \odot c_{t-1} + i_t \odot g_t \]

  *element-wise product*

- **Final hidden cell**:
  
  \[ h_t = o_t \odot \tanh(c_t) \]

**h_0, c_0 \in \mathbb{R}^h** are initial states (usually set to 0)
LSTMs: the formulation

- LSTMs has 4x parameters compared to simple RNNs:

Input dimension: $d$, hidden size: $h$

$$h_t = g(W h_{t-1} + U x_t + b) \in \mathbb{R}^h$$

$W \in \mathbb{R}^{h \times h}, U \in \mathbb{R}^{h \times d}, b \in \mathbb{R}^h$

$W^i, W^f, W^g, W^o \in \mathbb{R}^{h \times h}$

$U^i, U^f, U^g, U^o \in \mathbb{R}^{h \times d}$

$b^i, b^f, b^g, b^o \in \mathbb{R}^h$

Q: What is the range of the hidden representations $h_t$?
LSTMs: the formulation

- LSTM doesn’t guarantee that there is no vanishing/exploding gradient, but it does provide an easier way for the model to learn long-distance dependencies.

- LSTMs were invented in 1997 but finally got working from 2013-2015.
Gated Recurrent Units (GRUs)

- Introduced by Kyunghyun Cho in 2014:

Learning Phrase Representations using RNN Encoder–Decoder for Statistical Machine Translation

Kyunghyun Cho
Bart van Merriënboer
Caglar Gulcehre
Université de Montréal
firstname.lastname@umontreal.ca

Dzmitry Bahdanau
Jacobs University, Germany
d.bahdanau@jacobs-university.de

Fethi Bougares
Holger Schwenk
Université du Maine, France
Université de Montréal, CIFAR Senior Fellow
firstname.lastname@lium.univ-lemans.fr
find.me@on.the.web

- Simplified 3 gates to 2 gates: reset gate and update gate, without an explicit cell state
Gated Recurrent Units (GRUs)

- Reset gate:
  \[ r_t = \sigma(W^r h_{t-1} + U^r x_t + b^r) \]

- Update gate:
  \[ z_t = \sigma(W^z h_{t-1} + U^z x_t + b^z) \]

- New hidden state:
  \[ \tilde{h}_t = \tanh(W(r_t \odot h_{t-1}) + Ux_t + b) \]
  \[ h_t = (1 - z_t) \odot h_{t-1} + z_t \odot \tilde{h}_t \]

Q: What is the range of the hidden representations \( h_t \)?

Q: How many parameters are there compared to simple RNNs?
Let’s compare LSTMs and GRUs. Which of the following statements is correct?

(a) GRUs can be trained faster
(b) In theory LSTMs can capture long-term dependencies better
(c) LSTMs have a controlled exposure of memory content while GRUs don’t
(d) None of the above

All of these are correct (a) (b) (c) 😊
LSTMs vs GRUs

Music modeling

(Chung et al, 2014): Empirical Evaluation of Gated Recurrent Neural Networks on Sequence Modeling
LSTMs vs GRUs

Speech signal modeling

(Chung et al, 2014): Empirical Evaluation of Gated Recurrent Neural Networks on Sequence Modeling

https://imgflip.com/i/495iim
(only for fun!!!)
Recap: progress on language models

On the Penn Treebank (PTB) dataset
Metric: perplexity

<table>
<thead>
<tr>
<th>Model</th>
<th>#Param</th>
<th>Validation</th>
<th>Test</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mikolov &amp; Zweig (2012) - RNN-LDA + KN-5 + cache</td>
<td>9M</td>
<td>-</td>
<td>92.0</td>
</tr>
<tr>
<td>Zaremba et al. (2014) - LSTM</td>
<td>20M</td>
<td>86.2</td>
<td>82.7</td>
</tr>
<tr>
<td>Gal &amp; Ghahramani (2016) - Variational LSTM (MC)</td>
<td>20M</td>
<td>-</td>
<td>78.6</td>
</tr>
<tr>
<td>Kim et al. (2016) - CharCNN</td>
<td>19M</td>
<td>-</td>
<td>78.9</td>
</tr>
<tr>
<td>Merity et al. (2016) - Pointer Sentinel-LSTM</td>
<td>21M</td>
<td>72.4</td>
<td>70.9</td>
</tr>
<tr>
<td>Grave et al. (2016) - LSTM + continuous cache pointer</td>
<td>-</td>
<td>-</td>
<td>72.1</td>
</tr>
<tr>
<td>Inan et al. (2016) - Tied Variational LSTM + augmented loss</td>
<td>24M</td>
<td>75.7</td>
<td>73.2</td>
</tr>
<tr>
<td>Zilly et al. (2016) - Variational RHN</td>
<td>23M</td>
<td>67.9</td>
<td>65.4</td>
</tr>
<tr>
<td>Zoph &amp; Le (2016) - NAS Cell</td>
<td>25M</td>
<td>-</td>
<td>64.0</td>
</tr>
<tr>
<td>Melis et al. (2017) - 2-layer skip connection LSTM</td>
<td>24M</td>
<td>60.9</td>
<td>58.3</td>
</tr>
<tr>
<td>Merity et al. (2017) - AWD-LSTM w/o finetune</td>
<td>24M</td>
<td>60.7</td>
<td>58.8</td>
</tr>
<tr>
<td>Merity et al. (2017) - AWD-LSTM</td>
<td>24M</td>
<td>60.0</td>
<td>57.3</td>
</tr>
<tr>
<td>Ours - AWD-LSTM-MoS w/o finetune</td>
<td>22M</td>
<td>58.08</td>
<td>55.97</td>
</tr>
<tr>
<td>Ours - AWD-LSTM-MoS</td>
<td>22M</td>
<td>56.54</td>
<td>54.44</td>
</tr>
<tr>
<td>Merity et al. (2017) - AWD-LSTM + continuous cache pointer</td>
<td>24M</td>
<td>53.9</td>
<td>52.8</td>
</tr>
<tr>
<td>Krause et al. (2017) - AWD-LSTM + dynamic evaluation</td>
<td>24M</td>
<td>51.6</td>
<td>51.1</td>
</tr>
<tr>
<td>Ours - AWD-LSTM-MoS + dynamic evaluation</td>
<td>22M</td>
<td>48.33</td>
<td>47.69</td>
</tr>
</tbody>
</table>

(Yang et al, 2018): Breaking the Softmax Bottleneck: A High-Rank RNN Language Model
Are LSTMs and GRUs optimal?

\[ z = \text{sigm}(W_{xz}x_t + b_z) \]
\[ r = \text{sigm}(W_{xr}x_t + W_{hr}h_t + b_r) \]
\[ h_{t+1} = \tanh(W_{ih}(r \odot h_t) + \tanh(x_t) + b_h) \odot z + h_t \odot (1 - z) \]

\[ z = \text{sigm}(W_{xz}x_t + W_{hz}h_t + b_z) \]
\[ r = \text{sigm}(x_t + W_{hr}h_t + b_r) \]
\[ h_{t+1} = \tanh(W_{hh}(r \odot h_t) + W_{xh}x_t + b_h) \odot z + h_t \odot (1 - z) \]

\[ z = \text{sigm}(W_{xz}x_t + W_{hz} \tanh(h_t) + b_z) \]
\[ r = \text{sigm}(W_{xr}x_t + W_{hr}h_t + b_r) \]
\[ h_{t+1} = \tanh(W_{hh}(r \odot h_t) + W_{xh}x_t + b_h) \odot z + h_t \odot (1 - z) \]

\[
\begin{array}{|c|c|c|c|}
\hline
\text{Arch.} & \text{Arith.} & \text{XML} & \text{PTB} \\
\hline
\text{Tanh} & 0.29493 & 0.32050 & 0.08782 \\
\text{LSTM} & 0.89228 & 0.42470 & 0.08912 \\
\text{LSTM-f} & 0.29292 & 0.23356 & 0.08808 \\
\text{LSTM-i} & 0.75109 & 0.41371 & 0.08662 \\
\text{LSTM-o} & 0.86747 & 0.42117 & 0.08933 \\
\text{LSTM-b} & 0.90163 & 0.44434 & 0.08952 \\
\text{GRU} & 0.89565 & 0.45963 & 0.09069 \\
\text{MUT1} & 0.92135 & 0.47483 & 0.08968 \\
\text{MUT2} & 0.89735 & 0.47324 & 0.09036 \\
\text{MUT3} & 0.90728 & 0.46478 & 0.09161 \\
\hline
\end{array}
\]

\[
\begin{array}{|c|c|c|c|c|}
\hline
\text{Arch.} & 5\text{M-tst} & 10\text{M-v} & 20\text{M-v} & 20\text{M-tst} \\
\hline
\text{Tanh} & 4.811 & 4.729 & 4.635 & 4.582 (97.7) \\
\text{LSTM} & 4.699 & 4.511 & 4.437 & 4.399 (81.4) \\
\text{LSTM-f} & 4.785 & 4.752 & 4.658 & 4.606 (100.8) \\
\text{LSTM-i} & 4.755 & 4.558 & 4.480 & 4.444 (85.1) \\
\text{LSTM-o} & 4.708 & 4.496 & 4.447 & 4.411 (82.3) \\
\text{LSTM-b} & 4.698 & 4.437 & 4.423 & 4.380 (79.83) \\
\text{GRU} & 4.684 & 4.554 & 4.559 & 4.519 (91.7) \\
\text{MUT1} & 4.699 & 4.605 & 4.594 & 4.550 (94.6) \\
\text{MUT2} & 4.707 & 4.539 & 4.538 & 4.503 (90.2) \\
\text{MUT3} & 4.692 & 4.523 & 4.530 & 4.494 (89.47) \\
\hline
\end{array}
\]

(Jozefowicz et al, 2015): An Empirical Exploration of Recurrent Network Architectures
Comparison: FFNNs vs simple RNNs vs LSTMs vs GRUs

Feedforward NNs

Simple RNNs

LSTMs

GRUs

(a) (b) (c) (d)
A note on terminology

• Simple RNNs are also called vanilla RNNs

• Sometimes vanilla RNNs don’t work that well, so we need to use some advanced RNN variants such as LSTMs or GRUs

• In practice, we always use multi-layer RNNs

... together with fancy ingredients such as skip-connections with self-attention, variational dropout..

Slide credit: Abigail See (with modifications)
Practical takeaways

1. LSTMs are powerful
2. Clip your gradients
3. Use bidirectionality when possible
4. Multi-layer RNNs are more powerful, but you might need skip connections if it’s deep
A preview of assignment 3

- You will need to learn how to use PyTorch to train neural networks (on GPUs) for the named entity recognition (NER) task.
- We will ask you to implement FFNNs and LSTMs.

Ousted **WeWork** founder **Adam Neumann** lists his **Manhattan** penthouse for **$37.5 million**

[organization] | [person] | [location] | [monetary value]
A preview of assignment 3

**LINEAR**

CLASS `torch.nn.Linear(in_features, out_features, bias=True)`

Applies a linear transformation to the incoming data: $y = x^T A + b$

This module supports `TensorFloat32`.

**LSTM**

CLASS `torch.nn.LSTM(*args, **kwargs)`

Applies a multi-layer long short-term memory (LSTM) RNN to an input sequence.

For each element in the input sequence, each layer computes the following function:

- **input_size** – The number of expected features in the input $x$
- **hidden_size** – The number of features in the hidden state $h$
- **num_layers** – Number of recurrent layers. E.g., setting `num_layers=2` would mean stacking two LSTMs together to form a stacked LSTM, with the second LSTM taking in outputs of the first LSTM and computing the final results. Default: 1
- **bias** – If `False`, then the layer does not use bias weights $b_i$ or $b_h$. Default: `True`
- **batch_first** – If `True`, then the input and output tensors are provided as (batch, seq, feature). Default: `False`
- **dropout** – If non-zero, introduces a Dropout layer on the outputs of each LSTM layer except the last layer, with dropout probability equal to `dropout`. Default: 0
- **bidirectional** – If `True`, becomes a bidirectional LSTM. Default: `False`
- **proj_size** – If $> 0$, will use LSTM with projections of corresponding size. Default: 0

Make sure that you go to the precept this Friday if you are not familiar with PyTorch!!